Diphosphate structures related to the dichromate or thortveitite type

A. Boukhari

Laboratorie de Chimie du Solide Appliquée, Département de Chimie, Faculté des Sciences, Rabat (Morocco)

Abstract

The diphosphate structures $A_2P_2O_7$ contain P_2O_7 anions which show an eclipsed (dichromate-type) or staggered (thortveitite-type) spatial conformation. The first class is related to large ions A(II) (A = Ca, Sr, Ba, Cd, Pb), while the second family includes small cations (A = Mg, Mn, Fe, Co, Ni, Cu, Zn). In the mixed phosphates (A,B)₂P₂O₇, where A and B are bivalent ions, the type of structure is generally controlled by the largest cation.

1. Introduction

Compounds with the formula $R_2M_2O_7$ show a small number of groups of related structures [1, 2]. The size of the R^{n+} and $M^{(7-n)+}$ cations plays an important role in determining the type of crystalline structure. Thus, when the ionic radius of M is greater than about 0.5 Å, the observed structure types are pyrochlore [3] or weberite [4]. In this case the framework is built of interconnected MO_6 octahedra. However, if the ionic radius of M is less than 0.5 Å, two types of structures are known: the dichromate [5] and the thortveitite type [6, 7]. These compounds have been obtained with phosphorus, vanadium, silicon and chromium in their highest oxidation state [8–13]. They are characterized by isolated M_2O_7 groups made of two MO_4 tetrahedra sharing one corner.

The crystal structures of the diphosphates $A_2P_2O_7$, where A is a divalent cation, have been widely studied. The structure of materials with $A \equiv$ alkaline earth (Ca, Sr, Ba), Pb, Cd contains an eclipsed conformation of P_2O_7 anions [14–22] and is called dichromate (D) type. The second family corresponds to structures with bivalent metallic ions of small size ($A \equiv Mg$, Mn, Fe, Co, Ni, Cu, Zn) where the P_2O_7 ions have a staggered conformation [23–36]. Figure 1 shows the two spatial (eclipsed and staggered) geometries of P_2O_7 anions. The Cd₂P₂O₇ phosphate with the dichromate structure is the limit between the two families of dichromate and thortveitite type.

The size of A and B in $(A,B)_2P_2O_7$ compounds, where A and B are bivalent ions, plays a determining role in the P₂O₇ conformation. Therefore the following mixed compounds $(A,B)_2P_2O_7$ could be prepared.

(1) A and B are large ions; the parent $A_2P_2O_7$ and $B_2P_2O_7$ diphosphate structures are related to the dichromate family (A, B = Ca, Sr, Ba, Pb, Cd).



Fig. 1. (a) Eclipsed and (b) staggered conformation in dichromate- and thortveitite-type structures respectively.

(2) A and B have a small size (A, $B \equiv Mg$, Mn, Fe, Co, Ni, Cu, Zn); the A₂P₂O₇ and B₂P₂O₇ frameworks contain a staggered P₂O₇ conformation of the thortveitite type.

(3) A is large (A \equiv Ca, Sr, Ba, Pb, Cd) and B is a small cation (B \equiv Mg, Mn, Fe, Co, Ni, Cu, Zn); the parent phosphates A₂P₂O₇ and B₂P₂O₇ belong to the dichromate and thortveitite type respectively.

Our work deals with $A_2P_2O_7$ and $(A,B)_2P_2O_7$ singlecrystal structures related to the dichromate or thortveitite type and the influence of the cations A and B on the mixed frameworks with staggered or eclipsed P_2O_7 groups.

2. A₂P₂O₇ phosphates

2.1. Dichromate-related structures

The term "dichromate" results from the alkaline dichromate structure $K_2Cr_2O_7$ characterized by the eclipsed conformation of Cr_2O_7 [5].

The structures of $A_2P_2O_7$ phosphates of this family are made of basic units formed by two P_2O_7 groups related by an inversion or pseudoinversion centre of



Fig. 2. $(P_2O_7)_2$ basic unit in dichromate structures.



Fig. 3. $(P_2O_7)_2$ basic units observed in some diphosphate and dichromate structures of dichromate type.

symmetry. The two bridging oxygen atoms of the P– O–P links in the P_2O_7 groups are arranged in such a way as to obtain a close packing of them (Fig. 2).

Figure 3 shows the P_2O_7 units in some diphosphate and dichromate structures. The expansion of the basic units forms a zigzag infinite chain in the lattice (see *e.g.* Fig. 9). Figure 4 gives the projection on the (001) plane of α -Ca₂P₂O₇, which is a common structure for several diphosphates of the dichromate type [14], as we establish below.

Table 1 lists the allotropic forms and crystallographic data of diphosphates of the dichromate type. The P-O-P angle values of P_2O_7 groups in dichromate diphosphates $A_2P_2O_7$ (A = Ca, Sr, Ba, Pb, Cd) range from 128° to 138°.



Fig. 4. Structure of α -Ca₂P₂O₇ projected on (001) plane with Ca(1) and Ca(2) sites.

2.2. Thortveitite type

The structure of the mineral thortveitite, $(Sc, Y)_2 Si_2 O_7$, was determined by Zachariasen in the 1930s [7] and later refined by Cruickshank *et al.* [6]. The lattice is formed by isolated sheets of $Si_2 O_7$ anions parallel to the (001) plane. The scandium and yttrium cations are located between two adjacent sheets of $(Si_2 O_7^{6-})_n$. The Si-O-Si angle value is 180° for the staggered $Si_2 O_7^{6-}$ group.

Among the condensed diphosphates, several $A_2P_2O_7$ diphosphates (A = Mg, Mn, Fe, Co, Ni, Cu, Zn) crystallize with the thortveitite-type structure. They exhibit high temperature crystallographic forms except for A = Mn, Fe, Co.

The crystallographic data of $A_2P_2O_7$ phosphates with the thortveitite structure are listed in Table 2. The P-O-P angle values range from 137° to 180° (high symmetry).

3. (A,B)₂P₂O₇ diphosphates; A, B divalent cations

 $(A,B)_2P_2O_7$ crystal structures are less well known than their parent diphosphates $A_2P_2O_7$ and $B_2P_2O_7$, where A and B are bivalent ions. As reported above, the size of A and B has an important effect on the nature of the P_2O_7 conformation (staggered or eclipsed) in the lattice. Three possibilities can be discussed.

3.1. $(A,B)_2P_2O_7$ crystal structures; $A_2(B_2)P_2O_7$ of dichromate type

The mixed $(A,B)_2P_2O_7$ disphosphates of this family, reported with solved crystal structures, to our knowledge are PbBaP₂O₇ [37], CdBaP₂O₇ [38], Cd_{1.25}Ca_{0.75}P₂O₇ and CdSrP₂O₇ [39–41]. The two last compounds have been found as a particular composition in the solid solutions Cd_{2-x}Ca_xP₂O₇ and Cd_{2-x}Sr_xP₂O₇ respectively ($0 \le x \le 2$) and have been characterized by powder diffraction methods [39]. The

Α	Allotropic form	Space group; Z	Coordination number	P-O-P angle (deg)	Reference(s)
Ca	γ βª α	$P4_1; 8$ $P2_1/n; 4$	 7, 8, 9 8	130.5 137.8 131 128	14, 15
Sr	βª α ^b	P4 ₁ ; 8 Pbnm; 4	7, 8, 9 9	128 131 133.5	16-18
Ba	δ α ^ь	P6 ₃ – 3 Pbnm; 4		_	19
Cd		<i>P</i> 1; 2	5, 6	131.3	21
Pb		<i>P</i> 1; 4	8, 9	130 132	20

TABLE 1. Allotropic forms and crystallographic data of diphosphates A₂P₂O₇ of dichromate type

a, bIsotypical structures.

structures of PbBaP₂O₇ and CdBaP₂O₇ have been determined on single crystals. The former is isostructural with α -Ca₂P₂O₇.

X-ray diffraction analysis on powders of several compositions of the solid solution $Cd_{2-x}M_xP_2O_7$ (M = Ca, Sr) with $0 \le x \le 2$ shows different domains as indicated below

where A and A' are solid solutions isotypical with $Cd_2P_2O_7$, B and B' are solid solutions isotypical with α -Ca₂P₂O₇ and α -Sr₂P₂O₇ respectively, C and C' are solid solutions isotypical with $Cd_{1.25}Ca_{0.75}P_2O_7$ and $CdSrP_2O_7$ respectively and D and D' are mixtures of phases of adjacent domains C, B and A', C' respectively.

3.1.1. $M \equiv Ca$

Compounds of domains A $(0 \le x \le 0.40)$ and B $(1.70 \le x \le 2)$ are isomorphous to $Cd_2P_2O_7$ and α - $Ca_2P_2O_7$ respectively. Compounds with composition between 0.40 and 1.00 (domain C) show a solid solution of new phases of which the structure has been solved on a single crystal [40].

The evolution of density with the composition of domains A, B and C is presented in Fig. 5. A decrease

in the density is seen as Cd^{2+} ions are replaced by Ca^{2+} atoms.

3.1.2. $M \equiv Sr$

Domains A' and B' correspond to solid solutions isostructural with $Cd_2P_2O_7$ and α -Sr₂P₂O₇ respectively. The $CdSrP_2O_7$ (x = 1) structure solved on a single crystal is isomorphous to α -Ca₂P₂O₇. The variation in cell parameter values with the composition of domain B' is shown in Fig. 6.

Diphosphates synthesized in $Cd_{2-x}Sr_xP_2O_7$ solid solutions $(0 \le x \le 2)$ are closely related to the dichromate type as $Cd_2P_2O_7$ and $Sr_2P_2O_7$.

3.2. $(A,B)_2P_2O_7$ diphosphates; $A_2P_2O_7/B_2P_2O_7$ of dichromate/thortveitite type

This subsection deals with diphosphates $(A,B)_2P_2O_7$ where the pair $A_2P_2O_7/B_2P_2O_7$ corresponds to the dichromate/thortveitite type respectively.

Mixed structures of this type which have been determined using single-crystal data are as follows.

(1) SrNiP₂O₇ [42], CaCoP₂O₇ [43], BaCoP₂O₇, Ba-NiP₂O₇ [44], PbCoP₂O₇ [38], SrCoP₂O₇ and BaCuP₂O₇ [45]: these were found in the dichromate family with eclipsed P₂O₇ anions. Cations A of large size (A \equiv Ca, Sr, Ba, Cd, Pb) control the type of structure obtained.

(2) CaCuP₂O₇, SrCuP₂O₇ [46, 47] and CdCuP₂O₇ [48]: these structures are built of staggered P₂O₇ anions and are related to the thortveitite class. However, the first two compounds are isomorphous to α -Ca₂P₂O₇, while the last structure is characterized by mixed Cd– Cu sites (0.50:0.50). They are the first diphosphates which show that Cu²⁺, smaller in size than A²⁺

A	Allotropic form	Space group; Z	Coordination number	P-O-P angle (deg)	Reference(s)
Mg	α ^b βª	$B2_1/c; 8$ C2/m; 2	5, 6 6	144 180	26-28
Mn	а	C2/m; 2	6	180	34
Fe		C1; 2	6	180	35, 36
Co	b	$B2_{1}/c; 8$	5, 6	143.1	23
Ni	α ^ь β ^a γ σ	$B2_1/c; 8$ C2/m; 2 ; 8 $P2_1/a; 2$	5, 6 6 6	137 180 180 180	29-31
Cu	$lpha$ eta^{a}	C2/c; 4 C2/m; 2	5 6	157 180	24, 25
Zn	α	<i>I</i> 2/ <i>c</i> ; 12	5, 6	139 148	32, 33
	βª	C2/m; 2	6	180	

TABLE 2. Allotropic forms and crystallographic data of diphosphates $A_2P_2O_7$ of thortveitite type

^{a. b}Isotypical structures.



Fig. 5. Density variation with composition for domains A $(0 \le x \le 0.40)$, C (0.40 < x < 1.00) and B $(1.70 \le x \le 2)$ of Cd_{2-x}Ca_xP₂O₇ solid solution.

 $(A \equiv Ca, Sr, Cd)$, has influenced the framework, resulting in the thortveitite type, despite the expectation that larger A^{2+} ions should dominate the selection of the dichromate structure.

 $(Cd_{0.5}Cu_{0.5})_2 P_2O_7$ is a particular composition of the solid solution $Cd_{2-x}Cu_xP_2O_7$, $0 \le x \le 2$. Two domains, A ($0 \le x \le 0.40$) and B ($1.60 \le x \le 2$), have been observed. The phases of domain A are isomorphous to $Cd_2P_2O_7$. Those of domain B have Xray spectra similar to those of α - or β -Cu₂P₂O₇ [48]. A linear variation in unit cell parameters is observed in domain A with changing Cd:Cu ratio. An increase in x leads to a decrease in the volume of the unit cell.

The diphosphates $SrCuP_2O_7$, $CaCuP_2O_7$, $SrCdP_2O_7$, $BaPbP_2O_7$ and $PbCoP_2O_7$, solved on single crystals and which are isomorphous to α -Ca₂P₂O₇, have the large ions located at Ca(1) sites, while the small atoms are



Fig. 6. Variation with x of the unit cell parameters in domain B' of $Cd_{2-x}Sr_xP_2O_7$ solid solution.

inserted at the Ca(2) sites in the lattice. This distribution could be associated with the size of the Ca(1) sites, where the more voluminous cations such as calcium (CaCuP₂O₇), strontium (SrCuP₂O₇, SrCdP₂O₇), barium (BaPbP₂O₇) or lead (PbCoP₂O₇) are found.

Figure 7 reports the variation in the P–O–P angle of the P₂O₇ groups vs. the mean radius $r((r_A + r_B)/2)$ of ABP₂O₇ phosphates isotypical with α -Ca₂P₂O₇. Values of r_A and r_B are taken from Shannon's data [49]. Oxygen coordinations of A and B are those observed in these structures. We observe an increase and linear variation in the P–O–P angle with an increase in r.



Fig. 7. P-O-P angle vs. mean radius r of ABP_2O_7 phosphates isotypical with α -Ca₂P₂O₇, where A and B are bivalent ions.

Small values are obtained with copper disphosphates, showing a strong deformation of P_2O_7 anions with the staggered conformation.

3.3. $(A,B)_2P_2O_7$; $A_2(B_2)P_2O_7$ of thortweitite type

Moqine and coworkers have synthesized and characterized powders of solid solutions $Mg_{2-x}Cu_xP_2O_7$, $0 \le x \le 2$ [46, 50]. They have obtained a continuous domain between x = 0.05 and 1.94 isomorphous to β -Cu₂P₂O₇ (or β -Mg₂P₂O₇). The two β forms are isotypical. (Mg,Cu)₂P₂O₇ α - β transition temperatures were determined using the differential thermal analysis technique. The β -Mg₂P₂O₇ form has been obtained at room temperature with about 2.5% Cu²⁺ ions in α -Mg₂P₂O₇, while β -Cu₂P₂O₇ mes stabilized with about 3% Mg²⁺ ions in α -Cu₂P₂O₇. The increase in the α - β transition temperature in solid solution is about 20 K (α , β -Mg₂P₂O₇) and 16 K (α , β -Cu₂P₂O₇) respectively.

Similar results have been observed with $Cu_{2-x}A_xP_2O_7$ solid solutions (A = Fe, Co, Ni; $0 \le x \le 2$), where the β -Cu₂P₂O₇ form was stabilized with the substitution of a small amount of copper by A ions [51].

No details of single-crystal data are known for $(A,B)_2P_2O_7$ diphosphates of the thortveitite type. We have developed in our laboratory a systematic synthesis

of mixed diphosphates with small ions (A, $B \equiv Mg$, Mn, Fe, Co, Ni, Cu, Zn). Thus CuFeP₂O₇, MnCuP₂O₇ and NiCuP₂O₇ single crystals have been obtained.

4. Other diphosphate structures

Diphosphates other than $(A,B)_2P_2O_7$ seen above are known to have eclipsed P_2O_7 units. These compounds could be associated with the dichromate family. The structures of $Na_{7.39}Ni_{4.24}(P_2O_7)_4$, $Na_{7.13}Mg_{4.36}(P_2O_7)_4$, $Na_2CuP_2O_7$ (two forms, I and II) [52] and $Na_2CoP_2O_7$ (two forms, I and II) [53] have been solved using single crystals.

4.1. $Na_{7.39}Ni_{4.24}(P_2O_7)_4$ and $Na_{7.13}Mg_{4.36}(P_2O_7)_4$ diphosphates

Isostructural (Na,Ni) and (Na,Mg) structures have been determined on single crystals [52]. The solid state structures are characterized by mixed NiO₆(MgO₆) and PO₄ polyhedra which delimit large tunnels where Na⁺ ions are located. Both structures contain (P₂O₇)₂ basic units found in the dichromate type. These diphosphates could be classified in the dichromate family.

4.2. $Na_2CuP_2O_7$ structures

 $Na_2CuP_2O_7$ diphosphate exists in two allotropic solid state forms, I and II. The structures of the two forms, determined on single crystals, show eclipsed P_2O_7 groups associated in pairs as has been seen above in the dichromate type.

 $Na_2CuP_2O_7(I)$ is closely related to α - $Ca_2P_2O_7$. The cell parameters are

Na₂CuP₂O₇(I):
$$P2_1/n, a = 13.494(3)$$
 Å,
 $b = 8.823(3)$ Å, $c = 5.108(2)$ Å,
 $\beta = 92.77(3)^{\circ}$

 α -Ca₂P₂O₇: P2₁/n, a = 12.66(1) Å, b = 8.542(8) Å,

$$c = 5.315(5)$$
 Å, $\beta = 90.3(1)^{\circ}$

The Na⁺ ions are inserted at Ca(1) and Ca(2) sites of the calcium diphosphates; however, the Cu²⁺ ions are located between two equivalent and adjacent P₂O₇ groups along the *c*-axis (Fig. 8). Figure 9 shows P₂O₇ chains linked together with Cu²⁺ ions along the [001] axis in the Na₂CuP₂O₇(I) structure.

4.3. Na₂CoP₂O₇

The crystal structures of two allotropic forms, (I, II) of $Na_2CoP_2O_7$ have been obtained [53]. Structures of the form I can be described as a framework composed of mixed CoO_6 and PO_4 polyhedra creating tunnels parallel to the [001] direction. The Na^+ ions are located in these tunnels. The four independent P_2O_7 groups



Fig. 8. Structure of Na₂CuP₂O₇(I) projected on (001) plane.



Fig. 9. $(CuP_2O_7)^{2-1}$ infinite chains of P_2O_7 groups along [001].

exist in a quasi-eclipsed conformation and are arranged in groups of two to form the basic units determined in dichromate structures. The form I of $Na_2CoP_2O_7$ belongs to the dichromate class of P_2O_7 complexes.

The form II structure is characterized by layers of mixed CoO_4 and PO_4 tetrahedra alternating with layers of Na⁺ ions. P₂O₇ exists in the eclipsed conformation and the framework shows no pairing of P₂O₇ groups. The structure is not of the dichromate family despite the eclipsed conformation of the P₂O₇ anion.

Acknowledgments

This work has been developed in collaboration with researchers E. M. Holt, F. Abraham, B. Elouadi, J. Aride, A. Berrada, A. Alaoui El Belghiti, A. Moqine, F. Erragh and A. El Merzouki. The author is indebted to the "National Science Foundation" for financial aid in partial fulfilment of the present work.

References

- 1 J. A. Baglio and J. N. Dann, J. Solid State Chem., 4 (1972) 87.
- 2 I. D. Brown and C. Calvo, J. Solid State Chem., 1 (1970) 179.
- 3 F. Jona, G. Shirane and R. Pepinsky, *Phys. Rev.*, 98 (1955) 903.
- 4 A. Bystrom, Ark. Kem. Miner. Geol. B, 18 (1944) 1.
- 5 J. K. Brandon and I. D. Brown, Can. J. Chem., 46 (1968) 933.
- 6 D. W. J. Cruickshank, H. Lynton and G. A. Barclay, Acta Crystallogr., 15 (1962) 491.
- 7 W. H. Zakariasen, Z. Kristallogr., 73 (1936) 1.
- 8 P. K. L. Au and C. Calvo, Can. J. Chem., 48 (1967) 890.
- 9 C. Calvo, Acta Crystallogr., 23 (1967) 289.
- 10 B. E. Robertson and C. Calvo, J. Solid State Chem., 1 (1970) 120.
- 11 R. D. Shannon and C. T. Prewitt, J. Solid State Chem., 2 (1970) 199.
- 12 Yu. I. Smolin. Sov. Phys. -- Crystallogr., 15 (1970) 36.
- 13 Yu. I. Smolin and Yu. F. Shepelev, Acta Crystallogr. B, 26 (1970) 484.
- 14 C. Calvo, Inorg. Chem., 7 (1968) 1345.
- 15 N. C. Webb, Acta Crystallogr., 21 (1966) 942.
- 16 J. C. Grenier and R. Masse, Bull. Soc. Fr. Minér. Crystallogr., XC (1967) 285.
- 17 L. O. Hangman, I. Jansson and C. Magneli, *Acta Chem. Scand.*, 22 (1968) 1419.
- 18 C. W. W. Hoffman and R. W. Mooney, J. Electrochem. Soc., 107 (1960) 854.
- 19 NBS (US) Monogr. 25, 16 (1979) 19.
- 20 D. F. Mullica, H. O. Perkins, D. A. Grossie, L. A. Boatner and B. C. Sales, J. Solid State Chem., 62 (1986) 371.
- 21 C. Calvo and P. K. L. Au, Can. J. Chem., 47 (1969) 3409.
- 22 NBS (US) Monogr. 25, 16 (1969) 26.
- 23 N. Krishnamachari and C. Calvo, Acta Crystallogr. B, 28
- (1972) 2883.
 24 B. E. Robertson and C. Calvo, *Acta Crystallogr.*, 22 (1968) 665.
- 25 B. E. Robertson and C. Calvo, Can. J. Chem., 46 (1968) 605.
- 26 C. Calvo, Acta Crystallogr., 23 (1967) 298.
- 27 C. Calvo, Can. J. Chem., 43 (1965) 1139.
- 28 K. Lukaszewicz, Bull. Acad. Polon. Sci., Sér. Sci. Chim., XV(2) (1967) 53.
- 29 K. Lukaszewicz, Bull. Acad. Polon. Sci., Sér. Sci. Chim., XV(2) (1967) 47.
- 30 A. Pietraszeko and K. Lukaszewicz, Bull. Acad. Polon. Sci. Sér. Chim., XV(4) (1968) 183.
- 31 R. Masse, J. C. Guitel and A. Durif, *Mater. Res. Bull.*, 14 (1979) 337.
- 32 B. E. Robertson and C. Calvo, J. Solid. State Chem., 1 (1970) 120.
- 33 C. Calvo, Can. J. Chem., 43 (1965) 1147.
- 34 T. Stefanidis and A. G. Nord, *Acta Crystallogr. C*, 40 (1984) 1995.
- 35 J. T. Hoggins, J. S. Swinnea and H. Steinfink, J. Solid. State Chem., 47 (1983) 278.
- 36 T. Stefanidis and A. G. Nord, Z. Kristallogr., 159 (1982) 255.
- 37 A. Alaoui El Belghiti, A. Boukhari and E. M. Holt, Acta Crystallogr. C, 47 (1991) 473.

- 38 A. Elmerzouki, A. Boukhari, E. M. Holt and A. Berrada, in preparation.
- 39 A. Alaoui El Belghiti, D.E.S. de 3éme Cycle, Rabat, 1990.
- 40 A. Alaoui El Belghiti, A. Boukhari and E. M. Holt, in preparation.
- 41 A. Alaoui El Belghiti, A. Boukhari and E. M. Holt, in preparation.
- 42 E. Elbali, A. Boukhari and E. M. Holt, unpublished results, 19xx.
- 43 D. Riou, P. Labbe and M. Goreaud, C.R. Acad. Sci. Paris, 307(II) (1988) 1751.
- 44 D. Riou, P. Labbe and M. Goreaud, C.R. Acad. Sci. Paris, 307(II) (1988) 903.

- 45 A. Moqine, A. Boukhari and E. M. Holt, Acta Crystallogr. C. in press.
- 46 A. Boukhari, A. Moqine and A. Flandrois, 87 (1990) 251.
- 47 D. Riou and M. Goreaud, Acta. Crystallogr. C, 46 (1990) 1191.
- 48 A. Alaoui El Belghiti, A. Boukhari and E. M. Holt, in preparation.
- 49 R. D. Shannon, Acta Crystallogr. A, 32 (1976) 751.
- 50 A. Moqine, Thèse de Doctorat d'Etat, Rabat, 1990.
- 51 A. Handizi, Certificat d'Etudes Approfondies, Rabat, 1991.
- 52 F. Erragh, D.E.S. de 3ème Cycle, Rabat, 1989.
- 53 F. Erragh, A. Boukhari, B. Elouadi and E. M. Holt, J. Cryst. Spectrosc. Res., 21(3) (1991) 321.